## Course 2E02 2015 (SF Engineers & MSISS & MEMS)

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Ι	Due: at the end of the tutorial

## Exercise 1

Find the matrix for the linear transformations T defined by the equations

- (i)  $w_1 = x_1, \quad w_2 = x_2 3x_1,$
- (ii)  $w_1 = -x$ ,  $w_2 = y + 2z$ ,  $w_3 = -z$ ,
- (iii)  $w_1 = x_4$ ,  $w_2 = x_4 + x_3$ ,  $w_3 = x_4 x_3 + x_2$ ,  $w_4 = x_4 + x_3 + x_2 x_1$ , and by the formulas
- (iv)  $T(x_1, x_2) = (x_1, x_2),$
- (v)  $T(x_1, x_2, x_3) = (x_3, x_1 + 2x_2, x_1 + 4x_2 + x_3, -2x_2, x_3, x_1).$

## Exercise 2

Find  $T(\mathbf{x}) = A\mathbf{x}$  for the matrix A and the vector  $\mathbf{x}$  whenever the product makes sense (i.e. the sizes of A and  $\mathbf{x}$  fit together):

(i) 
$$A = \begin{pmatrix} 0 & -1 \\ 1 & -1 \end{pmatrix}, \mathbf{x} = \begin{pmatrix} 2 \\ -2 \end{pmatrix},$$
  
(ii)  $A = \begin{pmatrix} 0 & 1 & -1 \\ 3 & 0 & -2 \end{pmatrix}, \mathbf{x} = \begin{pmatrix} -1 \\ 1 \\ 0 \end{pmatrix},$   
(iii)  $A = \begin{pmatrix} 1 & 2 & 1 \\ -1 & 4 & 1 \end{pmatrix}, \mathbf{x} = \begin{pmatrix} -15 \\ -4 \end{pmatrix}.$ 

## Exercise 3

Use matrix multiplication to find:

- (i) the reflection of the vector (3, 2) about the x-axis;
- (ii) the orthogonal projection of the vector (-1, 2) to the y-axis;
- (iii) the image of the vector (1, -2) under rotation through the angle  $\frac{\pi}{3}$  about the origin.
- (v) the image of the vector (2, 1, -1) under rotation through the angle  $\frac{\pi}{4}$  about z-axis.