November 27, 2017 Lecturer Dmitri Zaitsev

Course 2E01 2017 (SF Engineers & MSISS & MEMS)

S h e e t 8

Due: at the end of the tutorial

Exercise 1

Calculate the coordinates of $\mathbf{v} = (3, 2, -1)$ relative to the orthogonal basis

$$\{(2, 0, 0), (0, 2, 3), (0, 3, -2)\} :$$

(i) with respect to the standard dot product;

(ii) with respect to the inner product $\langle \mathbf{u}, \mathbf{v} \rangle = 4u_1v_1 + u_2v_2 + u_3v_3$ (check that the given basis is still orthogonal with respect to this inner product).

Exercise 2

Find the orthogonal projection of the vector $\mathbf{v}$ onto the plane spanned by the orthogonal basis $\{\mathbf{u}_1, \mathbf{u}_2\}$ (with respect to the standard dot product), where

$$\mathbf{u}_1 = (1, 2, 0), \quad \mathbf{u}_2 = (-2, 1, -1),$$

and

(i) $\mathbf{v} = (1, 0, 1)$;

(ii) $\mathbf{v} = (1, 1, 1)$.

Exercise 3

Use the Gram-Schmidt process to transform the given basis into orthogonal one:

(i) $\mathbf{u}_1 = (-2, 0)$, $\mathbf{u}_2 = (1, 3)$;

(ii) $\mathbf{u}_1 = (1, 0, -1)$, $\mathbf{u}_2 = (1, 0, 0)$, $\mathbf{u}_3 = (2, 1, -1)$.