

Course 2E01 2016 (SF Engineers & MSISS & MEMS)**S h e e t 6**

Due: at the end of the tutorial

Exercise 1

Find the rank and the nullity of the matrix:

(i) $\begin{pmatrix} 2 & -2 & -2 \\ -3 & 3 & 3 \end{pmatrix};$

(ii) $\begin{pmatrix} 4 & -3 & -3 \\ 2 & 1 & 1 \\ 3 & 0 & 0 \end{pmatrix}.$

Exercise 2

Calculate the length of $\mathbf{u} = (-1, 2, 0)$, the distance between \mathbf{u} and $\mathbf{v} = (0, 1, 0)$ and the angle between \mathbf{u} and \mathbf{v}

- (i) with respect to the standard dot product;
- (ii) with respect to the inner product given by $\langle \mathbf{u}, \mathbf{v} \rangle = 4u_1v_1 + u_2v_2 + 2u_3v_3$.

Exercise 3

Which of the following bases are orthogonal and which are orthonormal with respect to the standard dot product?

- (i) $(-2, 0), (0, 3);$
- (ii) $(0, 0, 1), (2, 2, 0), (-1, 1, 0);$
- (iii) $(-1, 0, 0), (0, -\frac{3}{5}, \frac{4}{5}), (0, \frac{4}{5}, \frac{3}{5}).$