## Course 2E01 2016 (SF Engineers & MSISS & MEMS)

Sheet 2

Due: at the end of the tutorial

## Exercise 1

Find the matrix for the linear transformations T defined by the equations

- (i)  $w_1 = x_1, \quad w_2 = 2x_2 x_1,$
- (ii)  $w_1 = -y$ ,  $w_2 = y + 2z$ ,  $w_3 = -x$ , and by the formulas
- (iii)  $T(x_1, x_2) = (-x_2, x_1)$ .
- (iv)  $T(x_1, x_2, x_3) = (x_3, x_1 + x_2, x_1 + 4x_2 + x_3, -2x_1, x_3).$

## Exercise 2

Find  $T(\mathbf{x}) = A\mathbf{x}$  for the matrix A and the vector  $\mathbf{x}$  whenever the product makes sense (i.e. the sizes of A and  $\mathbf{x}$  fit together):

(i) 
$$A = \begin{pmatrix} 0 & -1 & 0 \\ 1 & -1 & 5 \end{pmatrix}$$
,  $\mathbf{x} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$ ,

(ii) 
$$A = \begin{pmatrix} 0 & 1 & -1 \\ 1 & 0 & 3 \end{pmatrix}$$
,  $\mathbf{x} = \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix}$ ,

## Exercise 3

Use matrix multiplication to find:

- (i) the reflection of the vector (2, -1) about the x-axis;
- (ii) the orthogonal projection of the vector (1, -1) to the y-axis;
- (iii) the image of the vector (1,2) under a rotation through the angle  $\frac{-\pi}{3}$  about the origin.
- (v) the image of the vector (1, -2, 5) under a rotation through the angle  $\frac{\pi}{4}$  about z-axis.
- (v) the image of the vector (1, -2, 3) under a dilation with factor 2.