

changing the direction of the rows means that they run in the x -direction. Each row starts at $x=0$, but to find its other end, we must invert $y = 4 - x^2$ to get $x = \sqrt{4-y}$.

So the inner integral, to work out the volume of each row, is $\int_0^{\sqrt{4-y}} \frac{x e^{2y}}{4-y} dx$.

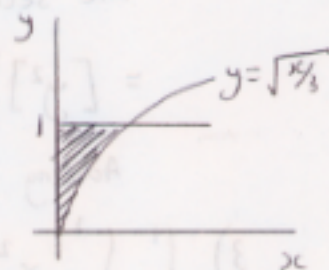
Including the outer integral, which sums over the rows, gives

$$\int_0^4 \int_0^{\sqrt{4-y}} \frac{x e^{2y}}{4-y} dx dy.$$

$$\begin{aligned} \int_0^4 \int_0^{\sqrt{4-y}} \frac{x e^{2y}}{4-y} dx dy &= \int_0^4 \left[\frac{\frac{1}{2} x^2 e^{2y}}{4-y} \right]_0^{\sqrt{4-y}} dy = \int_0^4 \frac{\frac{1}{2} e^{2y}}{4-y} dy \\ &= \left[\frac{1}{4} e^{2y} \right]_0^4 = \frac{1}{4} (e^8 - 1) \end{aligned}$$

$$5) \int_0^3 \int_{\sqrt{y/3}}^1 e^{y^3} dy dx$$

Again, here the rows run in the y -direction from the curve $y = \sqrt{x/3}$ up to the line $y=1$.



changing the direction, so that they run in the x -direction, means that they must run from $x=0$ to $x=3y^2$ ($3y^2$ is what we get when we rearrange $y = \sqrt{x/3}$). This gives,

$$\int_0^1 \int_0^{3y^2} e^{y^3} dx dy.$$

$$\begin{aligned} \int_0^1 \int_0^{3y^2} e^{y^3} dx dy &= \int_0^1 [x e^{y^3}]_0^{3y^2} dy = \int_0^1 3y^2 e^{y^3} dy \\ &= [e^{y^3}]_0^1 = e - 1. \end{aligned}$$