

MAU22C00 Assignment 8, Due Friday 24 November 2023

1. Find all the monoid homomorphisms from $(\mathbb{N}, +)$, i.e. the monoid whose set is natural numbers and whose operation is addition, to itself.
Hint: Describe them in terms of what value the function takes at 1.
2. Give a left regular grammar and a right regular grammar for the language of strings of x's and y's. In other words a string should be generated by the grammar if and only if every character in it is an x or a y. This is vacuously true of the empty string, so it should be generated by your language.
3. Give a left regular grammar for the language of those strings of x's, y's or z's which have no occurrence of x, no occurrence of y, or no occurrence of z. In case it's not obvious, by this I mean that there is at least one of the letters, x, y, or z which does not appear in the string; I don't mean that none of them appear.