

MA4447 The Standard Model

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1 Introduction

The Standard Model (SM) of elementary particle physics. Assignment during reading week worth 1/10th. There are things on the webpage www.maths.tcd.ie/~sint etc. look there for book list. SM is unchanged since 1978 so books from 89s are still ok to read:

- Griffiths
- Aitchinson and Hey
- Halzon and Martin
- D.H. Perkins, but this has emphasis on experimental techniques
- Peskin and Schroder QFT
- Bjorken and Drell, relativistic QM (vol1), QFT (vol2)
- Itzykson and Zuber, QFT

1.1 SM

- is the essence of 100 years of experiments and theoretical developments

- describes all experiments carried out to date with good to extremely high precision ¹
- Gravity is excluded in the SM

Phenomenological argument for excluding gravity in microscopic physics.

$$F_G = G_N \frac{m_e}{r^2}$$

$$F_{Coulomb} = \frac{1/abs e^2}{r^2}$$

$$\frac{F_G}{F_{Coulomb}} = O^{-10}$$

SM can be specified by an action or a Lagrangian density

$$S_{SM} = \int d^4x \mathcal{L}_{SM}(x)$$

$$\mathcal{L}_{SM}(x) = \mathcal{L}_{quarks}(x) + \mathcal{L}_{gauge}(x) + \mathcal{L}_{Higgs}(x) + \mathcal{L}_{Yukawa}(x)$$

$$\mathcal{L}_{quarks}(x) = \sum_{i=1}^3 \bar{\Psi}_{q_i}(x) \bar{D} \Psi_{q_i}(x)$$

$$\Psi_q = \begin{pmatrix} u \\ d \end{pmatrix}, \begin{pmatrix} c \\ s \end{pmatrix}, \begin{pmatrix} t \\ b \end{pmatrix} \bar{D} = \gamma_\mu D^{\mu 2} \in of W^\pm, Z^0, \gamma$$

$$\mathcal{L}_{leptons}(x) = \sum_{i=1}^3 \bar{\Psi}_{e_i} \bar{D} \Psi_{e_i}$$

$$\Psi_{e_i} = \begin{pmatrix} \nu_e \\ e^- \end{pmatrix}, \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}, \begin{pmatrix} \nu_\tau \\ e^- \end{pmatrix} \bar{D} \in of as above no gluons$$

$$\mathcal{L}_{gauge}(x) = -\frac{1}{4} \sum_{a=1}^8 G_{\mu\nu}^a G^{a\mu\nu} - \frac{1}{4} \sum_{a=1}^8 W_{\mu\nu}^a W^{a\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu}$$

$$\mathcal{L}_{Higgs}(x) = D_\mu \Phi^\dagger D^\mu \Phi - V(\Phi) D_\mu \text{element of above}$$

$$\Phi = (vertical matrix)(\Phi_1, \Phi_2), of complex scalar fields$$

$$\mathcal{L}_{Yukawa}(x) = \sum_{A,B=1}^3 y_{AB}^u \bar{\Psi}_{q_A} P_L \Phi P_R (v, c, t)_B$$

¹anomalous magnetic moment of muon good to 10⁹, though current experiments show neutrinos may have broken the temporal limit of the universe. A joke is: The barman says Sorry we don't serve neutrinos here, A neutrino walks into the bar, violation of causality

²covariant derivative

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