MAU11S02 sixth Monday quiz, week 8 Monday 22/3/21 due 4pm Monday 29/3/21

Rules and procedures.

1. Attempt 3 questions. Only your first three answers will be marked. 2. Each question carries 20 marks, so the maximum quiz mark is 60. 3. If a particular method of solution is stipulated, you get no marks if you don't use it. 4. Show all work. No marks will be given for answers which do not show the calculations. 5. Your answers should be scanned and submitted to Blackboard as a 'Monday assignment.'

Question 1. Calculate the least-squares linear estimate y = mx + c for the data

$$(-3,2), (-2,1), (-1,1), (1,1)$$

Question 2. Calculate the least-squares quadratic estimate $y = ax^2 + bx + c$ for the data in Question 1.

Question 3. Let

$$A = \begin{bmatrix} -5 & 2 \\ -28 & 10 \end{bmatrix}$$

Calculate eigenvalues and eigenvectors for A.

Question 4. Hence express A in the form $SA'S^{-1}$ where A' is a diagonal matrix, and evaluate e^A .

Question 5. With S, A, A' as above, evaluate $\cos(A\pi/6)$. (Recall $\cos x = 1 - x^2/2! + x^4/4! \dots$ and refer to the connection between e^A and $e^{A'}$ in the notes.)