MAU11S02 Group A2 Quiz 04 3pm 19/2/20

Rules and procedures.

1. Answers must be handed up at the end of the tutorial, no other time. 2. Attempt 3 questions. Only your first three answers will be marked. 3. Each question carries 20 marks, so the maximum quiz mark is 60. 4. Marked quizzes will be returned, and answers published, the following week. 5. If a particular method of solution is stipulated, you get no marks if you don't use it. 6. The (9) quizzes will contribute 20% to your overall mark. 7. You are allowed to collaborate and compare answers during the tutorial. 8. Show all work. No marks will be given for answers which do not show the calculations.

Question 1.

Calculate bases for the row space, column space, and nullspace of the following matrix

$$\left[\begin{array}{ccc}
1 & 0 & 6 \\
3 & -1 & 17 \\
1 & 1 & 7
\end{array}\right]$$

Question 2. Calculate a basis for the space of all linear combinations

$$\{\alpha_1(1,1,7) + \alpha_2(1,0,6) + \alpha_3(3,-1,17) : \alpha_1,\alpha_2,\alpha_3 \in \mathbb{R}\}\$$

Question 3. Calculate bases for the row and column spaces of the following matrix

$$\begin{bmatrix}
2 & 4 & 0 & 0 & 8 \\
3 & 6 & 0 & 1 & 13 \\
0 & 0 & 1 & -1 & 3 \\
3 & 6 & 0 & 3 & 15
\end{bmatrix}$$

Question 4. Calculate a basis for the nullspace of the matrix in Question 3.

Question 5. Do the three polynomials

$$(x-1)^2, x^2, (x-1)(x+1)$$

form a basis for the space of all polynomials of degree ≤ 2 ? Explain your answer, with calculations.