

## MAU11602 first quiz, week 2

Thu 11/02/21 due 11am Friday 19/02/21

### Rules and procedures.

1. Attempt 3 questions. Only *your first three answers* will be marked.
2. Each question carries 20 marks, so the maximum quiz mark is 60.
3. If a particular method of solution is stipulated, you get no marks if you don't use it.
4. **Show all work.** No marks will be given for answers which do not show the calculations.
5. Your answers should be scanned and submitted to Blackboard.

All turing machines must conform to the pattern required for the turinginC program. Also, if and when a machine terminates, the square being scanned should contain the leftmost nonblank tape symbol (blank if the tape is blank).

Question 1. There is a machine for incrementing binary strings on the web page. Modify it so that it loops on empty input.

Question 2. Present a Turing machine which, on input  $x$  (a bitstring), halts with  $|x| \bmod 2$  (0/1) on the tape.

Question 3. Present a Turing machine which halts with empty tape if the input  $x$  has the same number of occurrences of 0 as of 1, and loops otherwise.

Question 4 Present a Turing machine which on input  $x$  halts with  $x^R$  on the tape, where  $x^R$  is the reversal of  $x$ .

Question 5. Prove that if  $u, v, x, y$  are bitstrings and  $u, v$  are valid encodings of Turing machines and  $ux = vy$ , then  $u = v$  and  $x = y$ .