

Functions + routines.

`int` `main` (`int argc, char *argv[]`)
↑ ↑
 $\langle \text{return type} \rangle$ $\langle \text{name} \rangle$ $\underbrace{\hspace{8em}}_{\langle \text{arguments} \rangle}$

{ body of fn / routine :
 <local variables>, <statements> }

a routine is a function whose return type is void (does something, returns nothing).

atoi() } functions printf : routine.
atof()
scanf()

Trivial example

```
#include <stdio.h>
```

```
void show (int n)
```

```
{ printf("n is odd\n", n); }
```

```
int main()
```

```
{ show(45); }
```

GCD:

```
#include <stdio.h>
#include <stdlib.h>
int gcd(int m, int n)
{ int x = abs(m), y = abs(n), z;
  while (y > 0)
  { z = x % y; x = y; y = z; }
  return x;
}
int main()
{ int m, n;
  while (scanf("%d %d", &m, &n) == 2)
  { printf("gcd(%d, %d) is %d\n",
          m, n, gcd(m, n));
  }
}
```

Arguments and local variables.

In gcd function

m, n are arguments

x, y, z are local variables

Variables and arguments

in other **routines** (short for routine/function)
sharing any of these names m, n, x, y, z ,
are completely independent of them.

CALLING A ROUTINE

```
printf("gcd(%d,%d) is %d\n",  
      m,n, gcd(m,n));
```



call to gcd

(1) m, n in `main()`

copied to m, n in `gcd()`. COINCIDENCE.

(2) `gcd` is executed, - final value of x returned.

(3) that value is printed.

§ 12.7 makes clear that m in `main()` and in `gcd()` are independent.

§12.9 Boolean functions.

In (original) C, no boolean true/false.

int values used $\begin{cases} 0 = \text{false} \\ \text{nonzero} = \text{true} \\ \text{(usually, 1)} \end{cases}$

EG

```
int leapyear (int yy)
{ return yy % 4 == 0; }
```

```
int divides (int m, int n)
{ return (m != 0) && (n % m == 0); }
```

§12.9 Routine with array arguments

```
int total ( int n, int a[] )  
{ int s = 0;  
  int i;  
  for ( i = 0; i < n; ++i )  
    { s += a[i]; } // or s = s + a[i];  
  return s;  
} // returns a[0] + ... + a[n-1]
```

Simulate gcd(63, 35)

while (y > 0) { z = x % y; x = y; y = z; } return
x; ...

m	n	x	y	z	y > 0?
63	35	63	35	28	yes
		35	28	7	yes
		28	7	0	yes
		7	0	.	no

return 7

Simulate total(3, {3,1,4})

...for (i=0; i<n; ++i) { s+=a[i]; } return s

n	a	s	i	i<n	a[i]
3	{3,1,4}				

0	0	y	3
---	---	---	---

3	1	y	1
---	---	---	---

4	2	y	4
---	---	---	---

8	3	N	
---	---	---	--

return 8

Simulate gcd(63, 35)

while (y > 0) { z = x % y; x = y; y = z; } return
x; ...

m	n	x	y	z	y > 0?
63	35	63	35		yes
			28		
	35		28		yes
			7		
	28		7		yes
			0		no
	7		0		

return 7

Simulate total(3, {3,1,4})

...for (i=0; i<n; ++i) { s+=a[i]; } return s

n	a	s	i	i<n	a[i]
3	{3,1,4}				

0	0	y	3
---	---	---	---

3	1	y	1
---	---	---	---

4	2	y	4
---	---	---	---

8	3	N	
---	---	---	--

return 8

Routines which call themselves: **RECURSIVE**

```
int gcd ( int m, int n)
{ if (n == 0)
  { return m; }
  else
  { return gcd(n, m % n); }
```

```
int total ( int n, int a[] )
{ if ( n <= 0 )
  { return 0; }
  else
  { return total (n-1, a) + a[n-1]; }
}
```

VARIOUS RECURSIVE ROUTINES

```
int gcd(int m, int n)
{ if (n == 0)
  { return m; }
  else
  { return gcd(n, m % n); }
}
```

$$\text{gcd}(m, n) = \text{gcd}(n, m \% n)$$

```
int total(int n, int a[])
{ if (n == 0)
  { return 0; }
  else
  { return total(n-1, a)
    + a[n-1]; }
}
```

$$\sum_{i < n} a_i = \left(\sum_{i < n-1} a_i \right) + a_{n-1}$$

```
int rec_print(int n)
{ if (n > 0)
  { rec_print (n/10);
    printf("%d", n%10);
  }
}
```

$$n = (a_k \dots a_0)_{10}$$
$$n/10 = (a_k \dots a_1)_{10}$$
$$n\%10 = a_0$$

'RUSSIAN PEASANT ALGORITHM'

```
int product (int m, int n)
{ if (n == 0)
  { return 0; }
  else
  { int p = product
    (m, n/2);
    if (n % 2 == 0)
    { return p + p; }
    else
    { return p + p + m; }
  }
}
```

If n is even, $n = 2k$ say
then $mn = mk + mk$

If odd, $2k+1$ say
then
 $mn = mk + mk + m.$

similar
method
for A^k

PRIME FACTORS.

```
void factorise ( int n)
{ int seems_prime = 1 ;
  int m;
  for ( m=2; seems_prime
        && m<n; ++m)
  { if (divides ( m, n) ) ← smallest divisor
    { seems_prime = 0 ; ← m is prime
      printf ( "└ %d", m ); ← n is composite
      factorise ( n/m ); ← recurse
    }
  }
  if (seems_prime)
  { printf ( "└ %d", n ); } ← n is prime.
}
```