

```

int hp( int a, int b)
{
    int p=1;
    int x=b;
    while (x%a==0)
    {
        p *= a;
        x /= a;
    }
    return p;
}

```

at i^{th} iteration,

$$p = a^i \text{ and } x = b/p$$

$$i = 0 \quad p = a^0 \quad x = b/1$$

Invariant. Say

$$p = a^i, \quad x = b/p.$$

If $x \% a \neq 0$ then

$$p = a^{i+1} \text{ and } x = (b/a^i)/a = b/p.$$

If $x \% a \neq 0$ then loop ends.

If the i^{th} iteration is last,

then a^i divides b but a^{i+1} does not.

returns highest power of a dividing p .