

```

int xxx ( int r)
{ int s=0;
  int i;
  for ( i=0; i < r; ++i)
  { s = s + 2*i + 1; }
  return s;
}

```

Invariant.  $i: s = i^2$

~~Pres~~  $i=0? \checkmark$

say true for i.

then  $s = i^2$

$s = s + 2i + 1$

$= (i+1)^2$

then  $i$  ~~be~~ is  
assigned  $i+1$

✓

```

int yyy ( int m, int n)
{ int int x, y, z;
  x=m; y=n;
  while (y > 0)
  { z = x % y;
    x=y; y=z; }
  return x;
}

```

Invariant.

Def  $\gcd(x, y)$  is largest int dividing  
 $x$  and  $y$ .

$\therefore \gcd(m, n) = \gcd(x, y)$ .

Fact.  $x, y > 0 \Rightarrow \gcd(x, y) = \gcd(y, x \bmod y)$

Initially  $\gcd(m, n) = \gcd(m, n) \checkmark$ .

Invariant. Given  $\gcd(x, y) = \gcd(m, n)$

After assignments we have  $x, y$  replaced  
by  $y, x \bmod y$ : and  $\gcd(y, x \bmod y)$   
 $= \gcd(x, y) = \gcd(m, n) \checkmark$ .