

**Mathematics 1E2 2006–07**  
**HW 6 Due 21/11/06**

Tutorial ...

Name: \_\_\_\_\_

ID: \_\_\_\_\_

(1)(10 marks) Find the least-squares approximating line for the data  $(0, 1)$ ,  $(2, 2)$ ,  $(4, 0)$ ,  $(6, 3)$ .

(2)(12 marks) Which of the following maps from  $E^2$  to  $E^2$  are linear? If not, why not?.

(i)  $(x, y) \mapsto (x + 1, y - 1)$  (ii)  $(x, y) \mapsto (x^2, x^2)$  (iii)  $(x, y) \mapsto (x + y, x - y)$

(3)(10 marks) Construct the matrix of the map which projects points orthogonally onto the line  $x + 2y = 0$ .

(4)(18 marks) Let  $P = (1, -3, -1)$ ,  $Q = (1, -2, 1)$ ,  $R = (-4, 10, 1)$ . Calculate the matrix of the linear map whose matrix with respect to the basis  $P, Q, R$  is

$$\begin{bmatrix} 1 & 2 & 1 \\ 0 & 2 & 3 \\ 0 & 0 & 2 \end{bmatrix}$$