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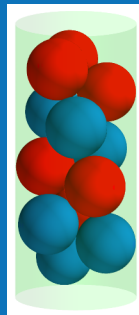
Coláiste na Tríonóide, Baile Átha Cliath  
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# Columnar structures: Packing spheres into cylinders

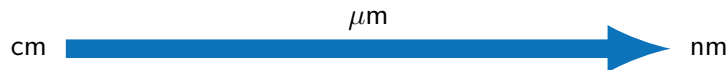
March 30, 2019 | Jens Winkelmann

*Co-authors:* A. Mughal, D. Weaire and S. Hutzler

“Packing and stacking  
we lay waste our days!”



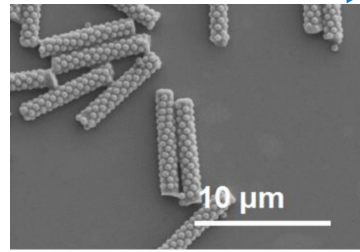
## Ordered columnar structure: Appearance from cm to nm!



Bushy Park,  
Dublin

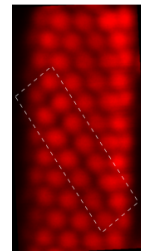


Foam



Micro-rods

Wu *et al.*; J Am Chem Soc 139, 5095–5101 (2017)



Optical  
metamaterial

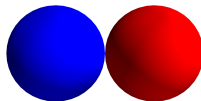
Tanjeem *et al.* (Harvard);  
Bull Am Phys Soc (2018)

Who ordered this?



## Simulation: Packing *soft* spheres into cylinders

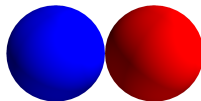
No overlap!



Hard spheres

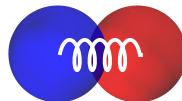
## Simulation: Packing *soft* spheres into cylinders

No overlap!



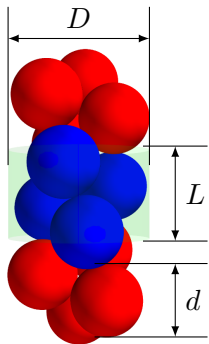
Hard spheres

$U(\delta_{ij}) \propto \text{overlap } \delta_{ij}^2$

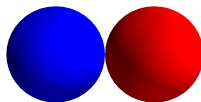


Soft spheres

## Simulation: Packing *soft* spheres into cylinders

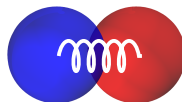


No overlap!



Hard spheres

$U(\delta_{ij}) \propto \text{overlap } \delta_{ij}^2$



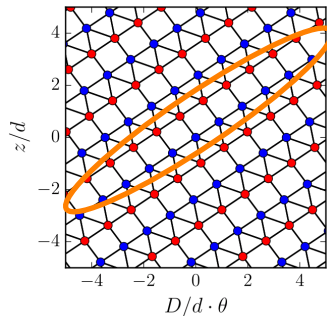
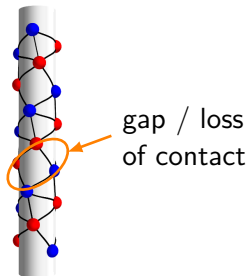
Soft spheres

- Generate structure at const pressure  $p$

$$\text{Enthalpy } H = \underbrace{U(\delta_{ij})}_{\text{internal energy}} + \underbrace{pV}_{\text{pressure} \times \text{volume term}}$$

**Enthalpy minimisation**

## What is a *line-slip* structure?



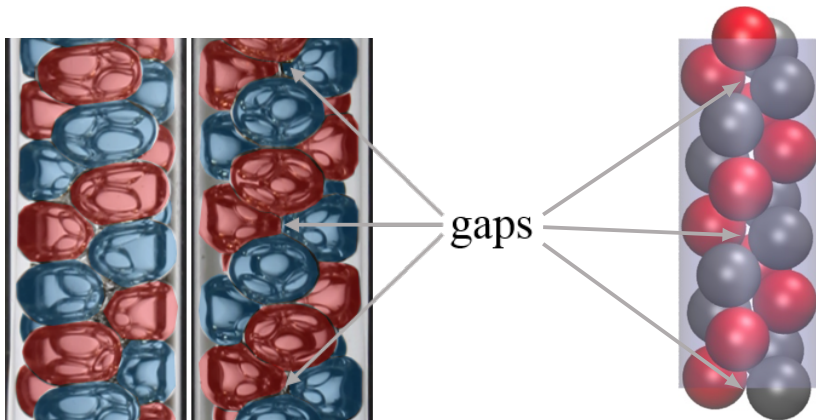
line-slip packing

Contact network

Rolled-out network

- Line slip is adjustable with pressure/compression
- For microrods: Stiffness/conductivity are adjustable by compression

## Experimental *line slip* in a foam




<sup>0</sup>Winkelmann et al; *Simulation and observation of line-slip structures in columnar structures of soft spheres*; Phys Rev E 97, 059902 (2017)

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