

Assignment 4

Maths 1124

Q1. Consider the transformation of $\mathbb{R} \times \mathbb{R}$ onto itself given by $(u, v) \rightarrow (x, y)$, where $x = au + bv$, $y = cu + dv$. Find conditions on (a, b, c, d) for this transformation to be bijective.

Q2. Prove that the set of all intervals (of length > 0), with both end points rational, is countable.

Q3. Prove that every family of disjoint intervals (of length > 0) is countable.

Q4. ~~Let $f: X \rightarrow Y$ be 1-1.~~
~~Prove $f(X \setminus Y) = f(X) \setminus f(Y)$.~~

Q4. Let $f: X \rightarrow Z$.
If $Y \subset X$ and f is 1-1
prove $f(X \setminus Y) = f(X) \setminus f(Y)$.
Is 1-1 necessary?