School of Mathematics

Course 373 — Finite Fields & Error-Correcting Codes 2001-02 (Optional JS & SS Mathematics, SS Two-subject Moderatorship)

Lecturer: Timothy Murphy & Michael Purser

Requirements/prerequisites: Knowledge of elementary Linear Algebra & Group Theory.

Duration: 21 weeks.

Number of lectures per week: 3

Assessment:

End-of-year Examination: One 3-hour examination

Description:

- **Part I:** The first part of the course, given by Dr Murphy, consists of algebraic preparation for the second and main part of the course, given by Dr Purser. This preparatory course will study:
 - The finite fields \mathbb{F}_{p^n} , their existence and uniqueness.

Part II: The second part of the course, given by Dr Purser, will cover:

- Introduction to codes, Hamming distance, etc.
- Linear block codes, parity check matrices, Hamming codes.
- Ideals and binary cyclic codes.
- Finite fields and BCH codes.
- Error-correcting techniques.
- Some examples: CCITT, Ethernet, EBU, GSM.
- Non-binary codes. Reed-Solomon codes.
- Convolutional Codes.
- Decoding of convolutional codes (Viterbi algorithm).
- Theoretical foundations of coding theory: Information Theory.
- Modelling channels, capacity and Shannon's theorem.
- Bounds and limits.
- Modulation and Signal/Noise Ratios.
- Soft-decision decoding.
- Trellis Code Modulation (TCM).
- Multi-level Block Code Modulation (MBCM).