

## School of Mathematics

**Course 471 — Quantum Computing**  
(JS & SS Mathematics )

2000-01

**Lecturer:** Professor T. C. Dorlas

**Requirements/prerequisites:** Linear Algebra and some computing experience.

**Duration:** 21 weeks

**Number of lectures per week:** 3

**Assessment:** End of year examination.

**End-of-year Examination:** 3-hour end of year exam?

### Description:

#### 1. Introduction to the basics of classical computing

Binary and hexadecimal numbers. Elements of assembly language for DOS.

Boolean logic. Definition of a Boolean ring. Various circuits: The full adder, binary decoders, multiplexers. flip-flops.

#### 2. Introduction to quantum mechanics.

The two-slit experiment. Plane waves. Probabilities and amplitudes. Dirac notation.

Spin and Stern-Gerlach experiment.

Hilbert space. Matrices and operators. Measurement and eigenvalues. Time evolution and the Schrodinger equation. Precession of spin. Pauli matrices and the magnetic Hamiltonian. Nuclear magnetic resonance.

#### 3. Quantum computing.

Definition of tensor product and qubits. Entanglement and the EPR experiment.

Quantum gates and quantum circuits. The controlled-NOT gate, the Toffoli gate and the Hadamard gate.

Universality and a proof of Deutch's theorem.

Quantum parallelism and quantum algorithms. Deutch's theorem and the Deutch-Jozsa promise problem; quantum algorithm and classical random algorithm. Simon's XOR problem.

Grover's search algorithm.

Introduction to factorisation of numbers and Schor's algorithm.

March 12, 2001