

## Exercise 13

### Pell's Equation

In exercises 1-10, find a non-trivial solution of the equation  $x^2 - dy^2 = 1$  for the given  $d$ .

- \*\* 1.  $d = 2$
- \*\* 2.  $d = 3$
- \*\* 3.  $d = 5$
- \*\* 4.  $d = 6$
- \*\* 5.  $d = 7$
- \*\*\* 6.  $d = 8$
- \*\*\* 7.  $d = 10$
- \*\*\* 8.  $d = 12$
- \*\*\* 9.  $d = 13$
- \*\*\* 10.  $d = 14$

In exercises 11-20, determine if the given equation has any solutions.

- \*\* 11.  $x^2 - 2y^2 = -1$
- \*\* 12.  $x^2 - 2y^2 = 2$
- \*\* 13.  $x^2 - 2y^2 = -1$
- \*\*\* 14.  $x^2 - 3y^2 = -1$
- \*\* 15.  $x^2 - 3y^2 = 2$
- \*\* 16.  $x^2 - 3y^2 = -2$
- \*\* 17.  $x^2 - 5y^2 = -1$
- \*\* 18.  $x^2 - 2y^2 = -1$
- \*\* 19.  $x^2 - 2y^2 = -1$
- \*\* 20.  $x^2 - 2y^2 = -1$
- \*\* 21.  $x^2 - 2y^2 = -1$