

**ON THE LINKING ALGEBRA OF HILBERT  
MODULES AND MORITA EQUIVALENCE OF  
LOCALLY  $C^*$ -ALGEBRAS**

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**Abstract.** In this paper we introduce the notion of linking algebra of a Hilbert module over a locally  $C^*$ -algebra and we extend in the context of locally  $C^*$ -algebras a result of Brown, Green and Rieffel [Pacific J., 1977] which states that two  $C^*$ -algebras are strongly Morita equivalent if and only if they are isomorphic with two complementary full corners of a  $C^*$ -algebra.

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