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On the structure of finite paramedial quasigroups

Comment.Math.Univ.Carolin. 51,2 (2010) 357–370.

Abstract: Information on the structure of finite paramedial quasigroups, including a classification of finite simple paramedial quasigroups, is given. The problem “Classify the finite simple paramedial quasigroups” was posed by J. Ježek and T. Kepka at the conference LOOPS’03, Prague 2003.

Keywords: quasigroup, paramedial quasigroup, medial quasigroup, simple quasigroup, idempotent

AMS Subject Classification: 20N05

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