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*On the structure of finite loop capable nilpotent groups*

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**Abstract:** In this paper we consider finite loops and discuss the problem which nilpotent groups are isomorphic to the inner mapping group of a loop. We recall some earlier results and by using connected transversals we transform the problem into a group theoretical one. We will get some new answers as we show that a nilpotent group having either  $C_{p^k} \times C_{p^l}$ ,  $k > l \geq 0$  as the Sylow  $p$ -subgroup for some odd prime  $p$  or the group of quaternions as the Sylow 2-subgroup may not be loop capable.

**Keywords:** loop, group, connected transversals

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