

Course 141: MECHANICS

Problem Set 1

Date Issued: October 24, 2007

Date Due: October 31, 2007

Each problem counts 5 points

1. Show that if $|\vec{A} - \vec{B}| = |\vec{A} + \vec{B}|$, then $\vec{A} \perp \vec{B}$.
2. Given two vectors \vec{A} , 5 units long and \vec{B} , 9 units long. What is the angle ϕ between \vec{A} and \vec{B} when $|\vec{A} + \vec{B}| = 7$?
3. Consider two points \vec{r}_1 and \vec{r}_2 separated by the distance $r = |\vec{r}_1 - \vec{r}_2|$. Find the vector \vec{R} from the origin to a point on the line between \vec{r}_1 and \vec{r}_2 at a distance kr from the point \vec{r}_1 , where k is some number such that $0 \leq k \leq 1$. State your answer in terms of k, \vec{r}_1 and \vec{r}_2 only. Sketch the vectors \vec{r}_1, \vec{r}_2 and \vec{R} .
4. A particle has the trajectory (in meters with t in seconds)

$$\vec{r}(t) = \cos t \hat{i} + \frac{t^2}{1+t} \hat{j}$$

- (a) Sketch the trajectory for $t \geq 0$.
 - (b) What is the maximum speed of the particle?
 - (c) What is the maximum acceleration of the particle?
5. A particle, moving in one dimension, has acceleration as shown below. The particle starts from rest at $t = 0$.
 - (a) Write down the particle's acceleration, $a(t)$, for $0 \leq t \leq 1$, $1 \leq t \leq 2$ and $t > 2$ seconds.
 - (b) Find the particle's velocity, $v(t)$, for any $t \geq 2$ seconds.