

Table of Laplace Transforms	
$f(t)$ for $t \geq 0$	$\mathcal{L}(f)$
1	$\frac{1}{s}$
e^{at}	$\frac{1}{s-a}$
t^n	$\frac{n!}{s^{n+1}} \ (n = 0, 1, \dots)$
$\sin at$	$\frac{a}{s^2 + a^2}$
$\cos at$	$\frac{s}{s^2 + a^2}$
$\sinh at$	$\frac{a}{s^2 - a^2}$
$\cosh at$	$\frac{s}{s^2 - a^2}$
$H_a(t)$	$\frac{e^{-as}}{s}$
$\delta(t-a)$	e^{-as}
$f'(t)$	$s\mathcal{L}(f) - f(0)$
$f''(t)$	$s^2\mathcal{L}(f) - sf(0) - f'(0)$

where

$$H_a(t) = \begin{cases} 0 & t \leq a \\ 1 & t > a \end{cases}$$

First shift theorem: If $\mathcal{L}(f(t)) = F(s)$ then

$$\mathcal{L}(e^{at}f(t)) = F(s-a).$$

Third shift theorem: If $\mathcal{L}(f(t)) = F(s)$ then

$$\mathcal{L}(H_a(t)f(t-a)) = e^{-as}F(s).$$