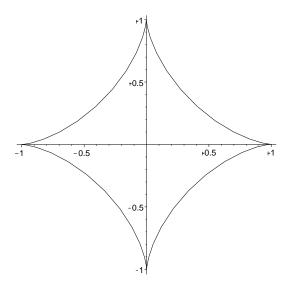
2E2 Tutorial Sheet 19 Third Term¹

$6~\mathrm{April}~2004$

- 1. (2) $\mathbf{a} = 3\mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$ and $\mathbf{b} = 2\mathbf{i} 9\mathbf{k}$. find $\mathbf{a} + \mathbf{b}$, $\mathbf{a} \cdot \mathbf{b}$ and $\mathbf{a} \times \mathbf{b}$. $\mathbf{c} = (0, 7, 2)$, find $\mathbf{a} \cdot \mathbf{c}$ and $\mathbf{b} \times \mathbf{c}$.
- 2. (3) $\mathbf{r}(t) = \sin \pi t^2 \mathbf{i} + \cos \pi t^2 \mathbf{j} + t^2 \mathbf{k}$ for $t \ge 0$ is a curve in space. Work out its length between its starting point, (0, 1, 0), and (0, -1, 1).



3. The figure shows the curve $\mathbf{r}(t) = \cos^3 t \mathbf{i} + \sin^3 t \mathbf{j}$. Work out its total length.

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