Origins of Modern Data Analysis Linked to the Beginnings and Early Development of Computer Science and Information Engineering

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Abstract

The history of data analysis that is addressed here is underpinned by two themes, – those of tabular data analysis, and the analysis of collected heterogeneous data. “Exploratory data analysis” is taken as the heuristic approach that begins with data and information and seeks underlying explanation for what is observed or measured. I also cover some of the evolving context of research and applications, including scholarly publishing, technology transfer and the economic relationship of the university to society.

1 Data Analysis as the Understanding of Information and Not Just Predicting Outcomes

1.1 Mathematical Analysis of Data

The mathematical treatment of data and information has been recognized since time immemorial. Galileo [20] expressed it in this way: “Philosophy is written in this immense book that stands ever open before our eyes (I speak of the Universe), but it cannot be read if one does not first learn the language and

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recognize the characters in which it is written. It is written in mathematical language, and the characters are triangles, circles, and other geometrical figures, without the means of which it is humanly impossible to understand a word; without these philosophy is confused, wandering in a dark labyrinth.” Plato is reputed to have had the phrase “Let no-one ignorant of geometry enter” at the entrance to his Academy, the school he founded in Athens [46].

1.2 Collecting Data

Large scale collection of data supports the analysis of data. Such collection is facilitated greatly by modern computer science and information engineering hardware, middleware and software. Large scale data collection in its own right does not necessarily lead to successful exploitation, as I will show with two examples, the VDI technical lexicon and the Carte du Ciel object inventory.

Walter Banjamin, 1882–1940, social and media (including photography and film) technology critic, noted the following, relating to engineering [5]. “Around 1900, the Verband Deutscher Ingenieure [German Engineers’ Association] set to work on a comprehensive technical lexicon. Within three years, index cards for more than three-and-a-half million words had been collected. But ‘in 1907 the association’s managing committee calculated that, with the present number of personnel, it would take forty years to get the manuscript of the technical lexicon ready for printing. The work was abandoned after it had swallowed up half a million marks’ [48]. It had become apparent that a technical dictionary should be structured in terms of its subject matter, arranged systematically. An alphabetical sequence was obsolete.” The “Carte du Ciel” (sky map) project was, in a way, similar. It was started in 1887 by Paris Observatory and the aim was to map the entire sky down to the 11th or 12th magnitude. It was planned as a collective and laborious study of photographic plates that would take up to 15 years. The work was not completed. There was a widespread view [27] that such manual work led to French, and European, astronomy falling behind other work elsewhere that was driven by instrumentation and new observing methods.

Over the past centuries, the mathematical treatment of data and information became nowhere more core than in physics. As Stephenson notes in his novel ([45], p. 689) – a point discussed by other authors elsewhere also – Isaac Newton’s “Principia Mathematica might never have come about had Nature not sent a spate of comets our way in the 1680s, and so arranged their trajectories that we could make telling observations.” Indeed the difficulties of experimentally verifying the theory of superstrings has led to considerable recent debate (e.g., recent books by P. Woit, Not Even Wrong; and L. Smolin, The Trouble with Physics).

1.3 Data Analysis and Understanding

I will move now to some observations related to the epistemology facets of data analysis and data mining. I use the cases of Gödel and of Benzécri to show
how earlier thinkers and scientists were aware of the thorny issues in moving from observed or measured data to the explanatory factors that underlie the phenomena associated with the data.

Logician Kurt Gödel, 1906–1978, had this critique to make of physics: “physics ... combines concepts without analyzing them” (p. 170, [50]). In a 1961 perspective he was able to claim: “... in physics ... the possibility of knowledge of objectivizable states of affairs is denied, and it is asserted that we must be content to predict the results of observations. This is really the end of all theoretical science in the usual sense.” (p. 140, [50].)

This was a view that was in many ways shared by the data analysis perspective espoused by data analyst and theorist, Jean-Paul Benzécri [8]: “... high energy theoretical physics progresses, mainly, by constituting corpora of rare phenomena among immense sets of ordinary cases. The simple observation of one of these ordinary cases requires detection apparatus based on millions of small elementary detectors. ...

Practitioners walk straight into the analyses, and transformations ... without knowing what they are looking for.

What is needed, and what I am proud about having somewhat succeeded in doing, is to see what is relevant in the objects studied, ...”

Philosopher Alain Badiou [4] (p. 79) echoes some of these perspectives on blindly walking into the analysis task: “empirical prodigality becomes something like an arbitrary and sterile burden. The problem ends up being replaced by verification pure and simple.”

The debate on the role of data analysis is not abating. In data analysis in neuroscience (see [32] or, as [22] states in regard to the neurogenetic basis of language, “studies using brain imaging must acknowledge that localization of function does not provide explanatory power for the linguist attempting to uncover principles underlying the speaker’s knowledge of language”), the issue of what explains the data analyzed is very often unresolved. This is notwithstanding solid machine or computer learning progress in being able to map characteristics in the data onto outcomes.

In this short discussion of data analysis, I am seeking solely to demarcate how I understand data analysis in this article. In general terms this is also what goes under the terms of: analyse des données in the French tradition; data mining; and unsupervised classification. The latter is the term used in the pattern recognition literature, and it can be counterposed to supervised classification, or machine learning, or discriminant analysis.

2 Beyond Data Tables: Origins of Data Analysis

2.1 Benzécri’s Data Analysis Project

For a few reasons I will begin with a focus on correspondence analysis. Following the best part of two years that I spent using multidimensional scaling and other methods in educational research, I started on a doctoral program in Benzécri’s
lab in 1978. I was very impressed by the cohesiveness of theoretical underpinning and breadth of applications there. Rather than an ad hoc application of an analysis method to a given problem, there was instead a focused and integrated view of theory and practice. What I found was far from being a bag of analytical tricks or curiosities. Instead the physics or psyche or social process lying behind the data was given its due. Benzécri’s early data analysis motivation sprung from text and document analysis. I will return to these areas in section 4.4 below.

The correspondence analysis and “aids to interpretation” research programs as well as software programs were developed and deployed on a broad scale in Benzécri’s laboratory at the Université Pierre et Marie Curie, Paris 6, through the 1970s, 1980s and 1990s. The hierarchical clustering programs distill the best of the reciprocal nearest neighbors algorithm that was published in the early 1980s in Benzécri’s journal, *Les Cahiers de l’Analyse des Données* (“Journal of Data Analysis”) and have not been bettered since then. (See also section 3.4 below.) Much of the development work in this framework, ranging from Einstein tensor notation through to the myriad application studies published in the journal *Les Cahiers de l’Analyse des Données*, were in an advanced state of development by the time of my arrival in Paris in late 1978 to start on a doctoral program.

A little book published in 1982, *Histoire et Préhistoire de l’Analyse des Données* [6], offers insights into multivariate data analysis or multidimensional statistics. It was written in the spring of 1975, circularized internally, published chapter-wise in *Les Cahiers de l’Analyse des Données*, before taking book form. It begins with a theme that echoes widely in Benzécri’s writings: namely that the advent of computers overturned statistics as understood up until then, and that the suppositions and premises of statistics had to be rethought in the light of computers. From probability theory, data analysis inherits inspiration but not methods: statistics is not, and cannot be, probability alone. Probability is concerned with infinite sets, while data analysis only touches on infinite sets in the far more finite world expressed by such a typical problem as discovering the system of relationships between rows and columns of a rectangular data table.

### 2.2 Tabular Data

With a computational infrastructure, the analysis of data tables has come into its own. Antecedents clearly go back much further. Therefore let me place the origins of data analysis in an unorthodox setting. Clark [13] cites Foucault [19] approvingly: “The constitution of tables was one of the great problems of scientific, political and economic technology in the eighteenth century ... The table of the eighteenth century was at once a technique of power and a procedure of knowledge”.

If tabular data led to data analysis, then it can also be pointed out that tabular data – in another line of evolution – led to the computer. Charles Babbage, 1791–1871, is generally avowed to be a father of the computer [47]. Babbage’s early (mechanical) versions of computers, his Difference Engine and Analyti-
cal Engine, were designed with tabular data processing in view, for example generating tables ranging from logarithms to longitude. “The need for tables and the reliance placed on them became especially acute during the first half of the nineteenth century, which witnessed a ferment of scientific invention and unprecedented engineering ambition – bridges, railways, shipbuilding, construction and architecture. ... There was one need for tables that was paramount – navigation. ... The problem was that tables were riddled with errors.” [47]. The computer was called for to avoid these errors.

2.3 Algorithmic and Computational Data Analysis

In discussing R.A. Fisher (English statistician, 1890–1962), Benzecri [6] acknowledges that Fisher in fact developed the basic equations of correspondence analysis but without of course a desire to do other than address the discrimination problem. Discriminant analysis, or supervised classification, took off in a major way with the availability of computing infrastructure. The availability of such methods in turn motivated a great deal of work in pattern recognition and machine learning. It is to be noted that computer-based analysis leads to a change of perspective with options now available that were not heretofore. Fisher’s brilliant approaches implicitly assume that variables are well known, and that relations between variables are strong. In many other fields, a more exploratory and less precise observational reality awaits the analyst.

With computers came pattern recognition and, at the start, neural networks. A conference held in Honolulu in 1964 on Methodologies of Pattern Recognition, that was attended by Benzecri, cited Rosenblatt’s perceptron work many times (albeit his work was cited but not the perceptron as such). Frank Rosenblatt (1928–1971) was a pioneer of neural networks, including the perceptron and neuromimetic computing which he developed in the 1950s. Early neural network research was simply what became known later as discriminant analysis. The problem of discriminant analysis, however, is insoluble if the characterization of observations and their measurements are not appropriate. This leads ineluctably to the importance of the data coding issue for any type of data analysis.

Psychometrics made multidimensional or multivariate data analysis what it has now become, namely, “search by induction of the hidden dimensions that are defined by combinations of primary measures”. Psychometrics is a response to the problem of exploring areas where immediate physical measurement is not possible, e.g. intelligence, memory, imagination, patience. Hence a statistical construction is used in such cases (“even if numbers can never quantify the soul!” [6]).

While it is now part of the history of data analysis and statistics that around the start of the 20th century interest came about in human intelligence, and an underlying measure of intelligence, the intelligence quotient (IQ), there is a further link drawn by Benzecri [6] in tracing an astronomical origin to psychometrics. Psychophysics, as also many other analysis frameworks such as the method of least squares, was developed in no small way by astronomers: the desire to penetrate the skies led too to study of the scope and limits of human
perception, and hence psychometrics.

Around the mid-1960s Benzécri began a correspondence with Roger N. Shepard which resulted in a visit to Bell Labs. Shepard (“a statistician only in order to serve psychology, and a psychologist out of love for philosophy”) and J. Douglas Carroll (who “joyfully used all his ingenuity – which was large indeed – to move data around in the computer like one would move perls in a kaleidoscope”) had developed proximity analysis, serving as a lynchpin of multidimensional scaling.

2.4 A Data Analysis Platform

The term “correspondence analysis” was first proposed in the fall of 1962. The first presentation under this title was made by J.-P. Benzécri at the Collège de France in a course in the winter of 1963.

By the late 1970s what correspondence analysis had become was not limited to the extraction of factors from any table of positive values. It also catered for data preparation; rules such as coding using complete disjunctive form; tools for critiquing the validity of results principally through calculations of contribution; provision of effective procedures for discrimination and regression; and harmonious linkage with cluster analysis. Thus a unified approach was developed, for which the formalism remained quite simple, but for which deep integration of ideas was achieved with diverse problems. Many of the latter originally appeared from different sources, and some went back in time by many decades.

Two explanations are proposed in [6] for the success of correspondence analysis. Firstly, the principle of distributional equivalence allows a table of positive values to be given a mathematical structure that compensates, as far as possible, for arbitrariness in the choice of weighting and subdivision of categories. Secondly, a great number of data analysts, working in very different application fields, found available a unified processing framework, and a single software package. Correspondence analysis was considered as a standard, unifying and integrated analysis framework – a platform.

2.5 Origins in Linguistic Data Analysis

Correspondence analysis was initially proposed as an inductive method for analyzing linguistic data. From a philosophy standpoint, correspondence analysis simultaneously processes large sets of facts, and contrasts them in order to discover global order; and therefore it has more to do with synthesis (etymologically, to synthesize means to put together) and induction. On the other hand, analysis and deduction (viz., to distinguish the elements of a whole; and to consider the properties of the possible combinations of these elements) have become the watchwords of data interpretation. It has become traditional now to speak of data analysis and correspondence analysis, and not “data synthesis” or “correspondence synthesis”.

The structural linguist Noam Chomsky, in the little volume, Syntactic Structures [12], held that there could not be a systematic procedure for determining
the grammar of a language, or more generally linguistic structures, based on a set of data such as that of a text repository or corpus. Thus, for Chomsky, linguistics cannot be inductive (i.e., linguistics cannot construct itself using a method, explicitly formulated, from the facts to the laws that govern these facts); instead linguistics has to be deductive (in the sense of starting from axioms, and then deriving models of real languages).

Benzécri did not like this approach. He found it idealist, in that it tends to separate the actions of the mind from the facts that are the inspiration for the mind and the object of the mind. At that time there was not available an effective algorithm to take ten thousand pages of text from a language to a syntax, with the additional purpose of yielding semantics. But now, with the advances in our computing infrastructure, statistics offers the linguist an effective inductive method for usefully processing data tables that one can immediately collect, with – on the horizon – the ambitious layering of successive research that will not leave anything in the shade – from form, meaning or style.

This then is how data analysis is feasible and practical in a world fueled by computing capability: “We call the distribution of a word the set of its possible environments.” In the background there is a consideration that Laplace noted: a well-constructed language automatically leads to the truth, since faults in reasoning are shown up as faults in syntax. Dijkstra, Wirth, Hoare and the other pioneering computer scientists who developed the bases of programming languages that we use today, could not have expressed this better. Indeed, Dijkstra’s view was that “the programmer should let correctness proof and program grow hand in hand” [17].

2.6 Information Fusion

From 1950 onwards, statistical tests became very popular, to verify or to protect the acceptability of a hypothesis (or of a model) proposed a priori. On the other hand correspondence analysis refers from the outset to the hypothesis of independence of observations (usually rows) $I$ and attributes (usually columns) $J$ but aims only at exploring the extent to which this is not verified: hence the spatial representation of uneven affinities between the two sets. Correspondence analysis looks for typical models that are achieved a posteriori and not a priori. This is following the application of mutual processing of all data tables, without restrictive hypotheses. Thus the aim is the inductive conjugating of models.

2.7 Benzécri’s and Hayashi’s Shared Vision of Science

If Benzécri was enormously influential in France in drawing out the lessons of data analysis being brought into a computer-supported age, in Japan Chikio Hayashi played no less a role. Hayashi (1918–2002) led areas that included public opinion research and statistical mathematics, and was first president of the Behaviormetric Society of Japan.

In [24] Hayashi’s data analysis approach is set out very clearly.
Firstly, what Hayashi referred to as “quantification” was the scene setting or data encoding and representation forming the basis of subsequent decision making. He introduced therefore [24] “methods of quantification of qualitative data in multidimensional analysis and especially how to quantify qualitative patterns to secure the maximum success rate of prediction of phenomena from the statistical point of view”. So, firstly data, secondly method, and thirdly decision making are inextricably linked.

Next comes the role of data selection, weighting, decorrelation, low dimensionality selection and related aspects of the analysis, and classification. “The important problem in multidimensional analysis is to devise the methods of the quantification of complex phenomena (intercorrelated behaviour patterns of units in dynamic environments) and then the methods of classification. Quantification means that the patterns are categorized and given numerical values in order that the patterns may be able to be treated as several indices, and classification means prediction of phenomena.” In fact the very aim of factor analysis type analyses, including correspondence analysis, is to prepare the way for classification: “The aim of multidimensional quantification is to make numerical representation of intercorrelated patterns synthetically to maximize the efficiency of classification, i.e. the success rate of prediction.” Factorial methods are insufficient in their own right, maybe leading just to display of data: “Quantification does not mean finding numerical values but giving them patterns on the operational point of view in a proper sense. In this sense, quantification has not absolute meaning but relative meaning to our purpose.”

This became very much the approach of Benzécri too. Note that Hayashi’s perspectives as described above date from 1954. In [7], a contribution to the journal Behaviormetrika that was invited by Hayashi, Benzécri draws the following conclusions on data analysis: “In data analysis numerous disciplines have to collaborate. The role of mathematics, although essential, remains modest in the sense that classical theorems are used almost exclusively, or elementary demonstration techniques. But it is necessary that certain abstract conceptions penetrate the spirit of the users, who are the specialists collecting the data and having to orientate the analysis in accordance with the problems that are fundamental to their particular science.” This aspect of integral linkage of disciplines is as aspect that I will return to in the Conclusions.

Benzécri [7] develops the implications of this. The advance of compute capability (remember that this article was published in 1983) “requires that Data Analysis [in upper case indicating the particular sense of data analysis as – in Hayashi’s terms and equally the spirit of Benzécri’s work – quantification and classification] project ahead of the concrete work, the indispensable source of inspiration, a vision of science.” Benzécri as well as Hayashi developed data analysis as projecting a vision of science.

He continues: “This vision is philosophical: it is not a matter of translating directly in mathematical terms the system of concepts of a particular discipline but of linking these concepts in the equations of a model. Nor is it a matter of accepting the data such as they are revealed, but instead of elaborating them in a deep-going synthesis which allows new entities to be discovered and simple
Finally, the overall domain of application of data analysis is characterized as follows: “Through differential calculus, experimental situations that are admirably dissected into simple components were translated into so many fundamental laws. We believe that it is reserved for Data Analysis to express adequately the laws of that which, complex by nature (living being, social body, ecosystem), cannot be dissected without losing its very nature.”

While Hayashi and Benzécri shared a vision of science, they also shared greatly a view of methodology to be applied. In a 1952 publication [23] Hayashi referred to “the problem of classification by quantification method” which is not direct and immediate clustering of data, but rather a careful combination of numerical encoding and representation of data as a basis for the clustering. Hayashi’s aim was to discuss: “(1) the methods of quantification of qualitative statistical data obtained by our measurements and observations ...; (2) ... the patterns of behaviour must be represented by some numerical values; (3) ... effective grouping is required.” Data analysis methods are not applied in isolation, therefore. In [7] Benzécri referred to correspondence analysis and hierarchical clustering, and indeed discriminant analysis (“so as not to be illusory, a discriminant procedure has to be applied using a first set of cases – the base set – and then trialled on other cases – the test set”).

In [7] Benzécri refers, just a little, to the breakthrough results achieved in hierarchical clustering algorithms around this time, and described in the work of Juan [28, 29]. These algorithmic results on hierarchical clustering were furthered in the following year by the work of de Rham [16]. As computational results they have not been bettered since and still represent the state of the art in algorithms for this family of classification method. In [33, 35, 36] I presented surveys of these algorithms relative to other fast algorithms for particular hierarchical clustering methods, and my software code was used in the CLUSTAN and R packages. More software code is available at [38]. In [34] I showed how, in practice, even more efficient algorithms can be easily designed.

3 The Changing University: Academe, Commercialization and Industry

3.1 The Growing Partnership of University and Industry

It is generally considered that a major milestone – perhaps the most important event – in propelling the university into the modern age was the Baye-Dole Act, brought into legislation in the United States, in 1980. It was a radical change in public polity perspective on the university and on research. Prior to then, the research role of universities was a public role, and research results were to be passed on to industry. Intellectual property was owned, prior to 1980, by the public purse, as embodied in the US Government. The Baye-Dole Act allowed universities to own intellectual property, to license it, and to otherwise exploit it as they saw fit. The university became a close partner of industry. It was a
change in legislation and in perception that echoed around the planet.

3.2 1968 in France: Role in Bringing the University Closer to Industry

The rise of the partnership between the university and industry, between academe and commercialization, that is now so integral, everywhere, had other facets too. Benzécri’s reflections [9] in this regard are of interest. In fact, these reflections throw a somewhat different light on the 1968 period of significant student and general social unrest.

Benzécri [9] paints the following picture.

“Forty years ago a memorable academic year started, the ravages of which are often deplored but also I must confess to having been the happy beneficiary. Charged by Prof. Daniel Dugué with the teaching of the Diplôme d’Études Approfondies (DEA) de Statistique – the Advanced Studies degree in Statistics, constituting the first part of a doctorate, I chose Data Analysis as the theme of the course. Prof. Dugué laughed and said this covered all of statistics! Under this broad banner, I intended to carry out lots of correspondence analyses. With such analyses, thanks to the patience of Brigitte Cordier, working on an IBM 1620 – a pocket calculator today but one that the Dean Yves Martin provided for the price of a chateau! – I was able, in Rennes, to aim at conquering linguistics, economics, and other fields.

To analyze, data were necessary. I was resolved to send the students of the DEA to collect sheafs of these precious flowers.

From my first class, I announced that the students should undertake internships. But this call, repeated from week to week, had no response. The students thought that, if they survived a written exam and an oral then no-one could ask them for more. Other than by cramming, they would have nothing to gain from the novelty of an excursion into practical things. Moreover, even if they accepted or even were enticed by my project then who would host their internship?

The pretty month of May 1968 would change all that!

Living in Orléans, I did not hear the shouting from Lutetia [i.e. from Paris and also from the university; Lutetia, or Lutèce, is the name of a town pre-existing Paris and the Arènes de Lutèce is a public park very close to Université Pierre et Marie Curie, Paris 6] but only distant echoes. Finally, in September, both boss and students had to resign themselves to each take back their role, each cautiously but also brazenly!

Since the month of May, the university was stigmatized as being arthritic, not offering a preparation for life. Not I but others had extolled internships. Machine-like of course the students came to tell me that they wanted to carry out internships. I had triumphed! Yes, yes, they stammered in confession, you had told us.

It was just so too for those who in November 1967 had refused any intern now in September 1968 were keen to save their native land by pampering young
people. The way opened up for correspondence analysis, a methodology that in practice was very soon associated with hierarchical clustering.”

3.3 The Changed Nature of the PhD

It is a source of some pride for me to be able to trace back through my doctoral lineage as follows [31]. My PhD advisor was Jean-Paul Benzécri. He studied with Henri Cartan (of Bourbaki; see [1] for a survey). Tracing back through advisors or mentors I have: Émile Borel and Henri Lebesgue; Simeon Poisson (advisor also to Gustav Dirichlet and Joseph Liouville); Joseph Lagrange (advisor also of Jean-Baptiste Fourier); Leonhard Euler; Johann Bernoulli; Jacob Bernoulli; and Gottfried Leibniz.

The PhD degree, including the title, the dissertation and the evaluation framework as a work of research (the “rite of passage”) came about in the German lands between the 1770s and the 1830s. Clark [13] finds it surprising that it survived the disrepute associated with all academic qualifications in the turmoil of the late 18th century. In the United States, the first PhD was awarded by Yale University in 1861. In the UK, the University of London introduced the degree between 1857 and 1860. Cambridge University awarded the DPhil or PhD from 1882, and Oxford University only from 1917.

A quite remarkable feature of the modern period is how spectacular the growth of PhD numbers has now become. In [40], I discuss how in the US, to take one example, in Computer Science and Engineering, the number of PhDs awarded has doubled in the three years to 2008. Internationally this evolution holds too. For example, Ireland is pursuing a doubling of PhD output up to 2013.

Concomitant with numbers of PhDs, the very structure of the PhD is changing in many countries outside North America. There is a strong movement away from the traditional German “master/apprentice” model, towards instead a “professional” qualification. This move is seen often as towards the US model. In Ireland there is a strong move to reform the PhD towards what is termed a “structured PhD”. This involves a change from the apprenticeship model consisting of lone or small groups of students over three years in one university department to a new model incorporating elements of the apprenticeship model centered around groups of students possibly in multiple universities where generic and transferable skills (including entrepreneurial) can be embedded in education and training over four years. Unlike in most of Europe, Germany is retaining a traditional “master/apprentice” model.

Numbers of PhDs are dramatically up, and in many countries there is a major restructuring underway of the PhD work content and even timeline. In tandem with this, in North America the majority of PhDs in such areas as computer science and computer engineering now move directly into industry when they graduate. This trend goes hand in hand with the move from an apprenticeship for a career in academe to, instead, a professional qualification for a career in business or industry.

In quite a few respects Benzécri’s lab was akin to what is now widely targeted
in terms of courses and large scale production of PhDs. I recall at the end of the 1970s how there were about 75 students *en thèse* – working on their dissertations – and 75 or so attending courses in the first year of the doctoral program leading to the DEA, Diplôme d’Études Approfondies, qualification. Not atypically at this time in terms of industrial outreach, I carried out a study for a company CIMSA, Compagnie d’Informatique Militaire, Spatiale et Aéronautique (a subsidiary of Thomson) on future computing needs; and my thesis was in conjunction with the Bureau de Recherches Géologiques et Minières, Orléans, the national geological research and development agency.

### 3.4 Changing Citation and Other Aspects of Scholarly Publication Practice

In my time in Benzécri’s lab, I developed a view of citation practice, relevant for mathematically-based PhD research in the French tradition, and this was as follows: a good introduction in a PhD dissertation in a mathematical domain would lay down a firm foundation in terms of lemmas, theorems and corollaries with derivation of results. However there was not a great deal of citing. Showing that one had assimilated very well the content was what counted, and not reeling off who had done what and when. On the other hand, it seemed to me to be relatively clear around 1980 that in general a PhD in the “Anglo-Saxon countries” would start with an overview chapter containing plenty of citations to the relevant literature (or literatures). This different tradition aimed at highlighting what one was contributing in the dissertation, after first laying out the basis on which this contribution was built.

Perhaps the divide was indicative just of the strong mathematical tradition in the French university system. However more broadly speaking citation practices have changed enormously over the past few decades. I will dwell a little on these changes now.

In a recent (mid-2008) review of citation statistics, Adler et al. [2] note that in mathematics and computer science, a published article is cited on average less than once; in chemistry and physics, an article is cited on average about three times; it is just a little higher in clinical medicine; and in the life sciences a published article is on average cited more than six times. It is small wonder therefore that in recent times (2008) the NIH (National Institutes of Health, in the US) has been a key front-runner in pushing Open Access developments – i.e. mandatory depositing of article postprints upon publication or by an agreed date following publication. The NIH Open Access mandate was indeed legislatively enacted [41].

In his use of *Les Cahiers de l’Analyse des Données*, a journal published by Dunod and running with 4 issues each year over 21 years up to 1997, Benzécri focused and indeed concentrated the work of his lab. Nowadays a lab- or even institute-based journal appears unusual even if it certainly testifies to a wide range of applications and activities. It was not always so. Consider e.g. the *Journal für die reine und angewandte Mathematik*, referred to as *Crelle’s Journal* in an earlier age of mathematics when August Leopold Crelle had founded...
it and edited it up to his death in 1855. Or consider, closer to Benzécri's lab, the *Annales de l’ISUP*, ISUP being the Institut Statistique de l’Université de Paris.

It is of interest to dwell here on just what scientific, or scholarly, publication is, given the possible insight from the past into current debates on Open Access, and citation-based performance and resource-allocation models in national research support systems.

As is well known what are commonly regarded as the first scientific journals came about in 1665. These were the Philosophical Transactions of the Royal Society of London early in that year and the Journal des Scavants in Paris a little later. Guédon [21] contrasts them, finding that “the Parisian publication followed novelty while the London journal was helping to validate originality”. The Philosophical Transactions was established and edited by Henry Oldenburg (c. 1619 to 1677), Secretary of the Royal Society. This journal “aimed at creating a public record of original contributions to knowledge”. Its primary function was not (as such) general communication between peers, nor dissemination to non-scientists, but instead “a public registry of discoveries”. This first scientific journal was a means for creating intellectual property. Journals originating in Oldenburg’s prototypical scientific – indeed scholarly – journal are to be seen “as registers of intellectual property whose functions are close to that of a land register”.

Noting parallels with the modern web age, Guédon [21] sees how in the 17th century, “the roles of writers, printers, and bookstore owners, as well as their boundaries, were still contentious topics.” The stationers sought to establish their claim, just like a claim to landed property. By defining authorship in the writing activity, and simultaneously the intellectual property of that author, the way was open to the stationer as early publisher to have the right to use this property analogous to landed property. Johns [26] points to how suspicion and mistrust accompanied early publishing so that Oldenburg was also targeting an “innovative use of print technology”. Guédon [21] finds: “The design of a scientific periodical, far from primarily aiming at disseminating knowledge, really seeks to reinforce property rights over ideas; intellectual property and authors were not legal concepts designed to protect writers – they were invented for the printers’ or stationers’ benefits.” Let me temper this to note how important intellectual property over ideas is additionally in terms of motivation of scholars in subsequent times.

The context as much as the author-scientist led to this particular form of intellectual property. What I find convincing enough in the role of the printer or stationer is that the article, or collection of articles in a journal, or other forms of printed product (pamphlet, treatise), became the most important paradigm. Other possible forms did not. Examples could include: the experiment; or the table of experimental data; or catalogs or inventories. Note that the latter have become extremely important in, e.g., observational data based sciences such as astronomy, or the processed or derived data based life sciences. What is interesting is that the publication remains the really dominant form of research output.
Coming now to authorship, there has been an overall shift toward teamwork in authorship, clearly enough led by the life sciences and by “big science”. In the highly cited journal, *Nature*, it has been noted [49] that “almost all original research papers have multiple authors”. Furthermore (in 2008), “So far this year ... *Nature* has published only six single-author papers, out of a total of some 700”. What is however very clear is that mathematics or statistics or related methodology work rarely ever appears in *Nature*. While social networks of scientists have become very important, notes Whitfield, nonetheless there is room still for a counter-current in scholarly activity: “... however finely honed scientists’ team-building strategies become, there will always be room for the solo effort. In 1963, Derek de Solla Price, the father of authorship-network studies, noted that if the trends of that time persisted, single-author papers in chemistry would be extinct by 1980. In fact, many branches of science seem destined to get ever closer to that point but never reach it.”

With online availability now of the scholarly literature it appears that relatively fewer, rather than more, papers are being cited and, by implication, read. Evans [18] finds that: “as more journal issues came online, the articles referenced tended to be more recent, fewer journals and articles were cited, and more of those citations were to fewer journals and articles”. Evans continues: “The forced browsing of print archives may have stretched scientists and scholars to anchor findings deeply into past and present scholarship. Searching online is more efficient and following hyperlinks quickly puts researchers in touch with prevailing opinion, but this may accelerate consensus and narrow the range of findings and ideas built upon.” Again notwithstanding the 34 million articles used in this study, it is clear that there are major divides between, say, mathematical methodology and large teams and consortia in the life and physical sciences.

In a commentary on the Evans article [18], Couzin [15] refers to “herd behavior among authors” in scholarly publishing. Couzin concludes by pointing to how this trend “may lead to easier consensus and less active debate in academia”.

I would draw the conclusion that mathematical thinking – if only because it lends itself poorly to the particular way that “prevailing opinion” and acceleration of “consensus” are forced by how we now carry out research – is of great importance for innovation and new thinking.

The change in research and scholarly publishing has implications for book publishing. Evans [18] notes this: “The move to online science appears to represent one more step on the path initiated by the much earlier shift from the contextualized monograph, like Newton’s *Principia* or Darwin’s *Origin of Species*, to the modern research article. The *Principia* and *Origin*, each produced over the course of more than a decade, not only were engaged in current debates, but wove their propositions into conversation with astronomers, geometers, and naturalists from centuries past. As 21st-century scientists and scholars use online searching and hyperlinking to frame and publish their arguments more efficiently, they weave them into a more focused – and more narrow – past and present.”

Undue focus and narrowness, and “herd behavior”, are at odds with the
Hayashi and Benzécri vision of science. Fortunately, this vision of science has not lost its sharp edge and its innovative potential for our times.

4 Centrality of Data Analysis in Early Computer Science and Engineering

4.1 Data Stores: Prehistory of the Web

Comprehensive and encyclopedic collection and interlinkage of data and information that is now typified by the web has a very long history. Here I first point to just some of these antecedents that properly belong to the prehistory, well avant la lettre, of the web.

In the 12th century the web could maybe be typified by the work of John Tzetzes, c. 1110–1180, who according to Browning [10] was somewhat dysfunctional in his achievements: “... His range was immense ... He had a phenomenal memory ... philological commentaries on works of classical Greek poetry ... works of scholarship in verse ... long, allegorical commentaries ... encyclopedia of Greek mythology ... long hexameter poems ... works of popularization ... Tzetzes compiled a collection of his letters, as did many of his contemporaries. He then went on, however, and equipped it with a gigantic commentary in nearly 13,000 lines of ‘political’ verse, which is a veritable encyclopedia of miscellaneous knowledge. Later he went on to add the elements of a prose commentary on his commentary. The whole work conveys an impression of scholarship without an object, of a powerful engine driving nothing. Tzetzes was in some ways a misfit and a failure in his own society. Yet his devotion of immense energy and erudition to a trivial end is a feature found elsewhere in the literature of the twelfth century, and points to a breakdown in the structure of Byzantine society and Byzantine life, a growing discrepancy between ends and means.”

In modern times, the famous 1945 article [11] by Vannevar Bush (1890–1974) set the scene in very clear terms for the web: “Consider a future device for individual use, which is a sort of mechanized private file and library. It needs a name, and, to coin one at random, ‘memex’ will do. A memex is a device in which an individual stores all his books, records, and communications, and which is mechanized so that it may be consulted with exceeding speed and flexibility. It is an enlarged intimate supplement to his memory.”

It is not widely recognized that Bush’s famous essay was preceded by an extensively developed plan by Belgian Paul Otlet, 1868–1944, especially in his book, Traité de Documentation [42], published in Brussels in 1934.

As described by him in the chapter entitled “The preservation and international diffusion of thought: the microphotic book” in [43], a clear view was presented (p. 208) of the physical, logical, and indeed socio-economical, layers necessary to support a prototype of the web: “By combining all the central offices discussed ... one could create a “Document Super-Center.” This would be in contact with national centers to which a country’s principal offices of documentation and libraries would be linked to form stations in a universal
network. ... The books, articles and documents ... would be brought together in a great collection. Gradually a classified Microphotic Encyclopedia would be formed from them, the first step toward new microphotolibraries. All of these developments would be linked together to form a Universal Network of Documentation.”

4.2 Between Classification and Search

In the next three sections, sections 4.3, 4.4 and 4.5, I progress through the physical and logical layers supporting data analysis. I detail just some of the work in the 1960s and 1970s that involved the practicalities of data analysis. Such work extended the work of Otlet and Bush. While constituting just small building blocks in the massive edifice of what we now have by way of search and access to data and information, the contribution of underpinning theory and of skillful implementation that I discuss in these sections should not be underestimated.

Let me draw a line between the work of Bush and Otlet, which may have been eclipsed for some decades, but which indicates nonetheless that certain ideas were in the spirit of the times. The disruptive technology that came later with search engines like Google changed the rules of the game, as the software industry often does. Instead of classifying and categorizing information, search and discovery were to prove fully sufficient. Both classification and search were a legacy of the early years of exploratory data analysis research. Classification and search are two sides of the same coin. Consider how the mainstay to this day of hierarchical clustering algorithms remain the nearest neighbor chain and reciprocal nearest neighbor algorithms, developed in Benzécri’s lab in the early 1980s [36].

The ftp protocol (file transfer protocol) was developed in the 1970s and took its definitive present form by 1985. Increasingly wider and broader uptake of data and information access protocols was the order of the day by around 1990. Archie, a search service for ftp was developed initially at the McGill University School of Computer Science in 1990. The World Wide Web concept and http (hypertext transfer protocol) was in development by Tim Berners-Lee at CERN by 1991. In 1991 a public version of Wide Area Information Servers (WAIS), invented by Brewster Kahle, was released by Thinking Machines Corporation WAIS was based on the Z39.50 and was a highly influential (certainly for me!) forerunner of web-wide information search and discovery. In April 1991 Gopher was released by the University of Minnesota Microcomputer, Workstation and Networks Center. Initially the system was a university help service, a “campus-wide document delivery system”. In 1992, a search service for Gopher servers was developed under the name of Veronica, and released by the University of Nevada. The University of Minnesota upset the burgeoning communities using wide area data and information search and discovery by introducing licensing of Gopher. This was just before the release of the Mosaic web browser, developed by Marc Andreessen, an undergraduate student at the University of Illinois, Champaign. A contemporary vantage point on some of these developments is...
in my edited compilation [25], which was finalized in the late summer of 1992.

It may be noted too that the bibliographies in the Classification Literature Automated Search Services (see Appendix) were set up to be accessed through WAIS in the early 1990s.

It is useful to have sketched out this subsequent evolution in data and information search and discovery because it constitutes one, but unquestionably an enormous, development rooted in earlier work on heterogeneous data collection and multivariate data analysis.

4.3 Environment and Context of Data Analysis

I have noted that even in early times, the role of computational capability was central (see sections 2 and 3.2).

Describing early work with John Gower in the Statistics Department at Rothamsted Experimental Station in 1961, when Frank Yates was head of department, Gavin Ross reviewed data analysis as follows [44].

"... we had several requests for classification jobs, mainly agricultural and biological at first, such as classification of nematode worms, bacterial strains, and soil profiles. On this machine and its faster successor, the Ferranti Orion, we performed numerous jobs, for archaeologists, linguists, medical research laboratories, the Natural History Museum, ecologists, and even the Civil Service Department.

On the Orion we could handle 600 units and 400 properties per unit, and we programmed several alternative methods of classification, ordination and identification, and graphical displays of the minimum spanning tree, dendrograms and data plots. My colleague Roger Payne developed a suite of identification programs which was used to form a massive key to yeast strains.

The world of conventional multivariate statistics did not at first know how to view cluster analysis. Classical discriminant analysis assumed random samples from multivariate normal populations. Cluster analysis mixed discrete and continuous variables, was clearly not randomly sampled, and formed non-overlapping groups where multivariate normal populations would always overlap. Nor was the choice of variables independent of the resulting classification, as Sneath had originally hoped, in the sense that if one performed enough tests on bacterial strains the proportion of matching results between two strains would reflect the proportion of common genetic information. But we and our collaborators learnt a lot from these early endeavours."

In establishing the Classification Society [14], the interdisciplinary of the objectives was stressed: "The foundation of the society follows the holding of a Symposium, organized by Aslib on 6 April, 1962, entitled 'Classification: an interdisciplinary problem', at which it became clear that there are many aspects of classification common to such widely separated disciplines as biology, librarianship, soil science, and anthropology, and that opportunities for joint discussion of these aspects would be of value to all the disciplines concerned."

How far we have come can be seen in [9] where target areas are sketched out that range over analysis of voting and elections; jet algorithms for the Tevatron
and Large Hadron Collider systems; gamma ray bursts; environment and climate management; sociology of religion; data mining in retail; speech recognition and analysis; sociology of natality – analysis of trends and rates of births; and economics and finance – industrial capital in Japan, financial data analysis in France, monetary and exchange rate analysis in the United States. In all cases the underlying explanations are wanted, and not superficial displays or limited regression modeling.

4.4 Information Retrieval and Linguistics: Early Applications of Data Analysis

Roger Needham and Karen Spärck Jones were two of the most influential figures in computing and the computational sciences in the UK and worldwide.

The work of Roger Needham, who died in February 2003, ranged over a wide swathe of computer science. His early work at Cambridge in the 1950s included cluster analysis and information retrieval. In the 1960s, he carried out pioneering work on computer architecture and system software. In the 1970s, his work involved distributed computing. In later decades, he devoted considerable attention to security.

In the 1960s he published on clustering and classification. Information retrieval was among the areas he contributed to. Among his early publications were:


Needham, who was the husband of Spärck Jones, set up and became first director of Microsoft Research in Cambridge in 1997.

Karen Spärck Jones died in April 2007. Among early and influential publications on her side were the following.


Even in disciplines outside of formative or emergent computer science, the centrality of data analysis algorithms is very clear from a scan of publications in earlier times. A leader of classification and clustering research over many decades is James Rohlf (State University of New York). As one among many examples, we note this work of his:


I will now turn attention to the early years of the Computer Journal.

4.5 Early Computer Journal

A leader in early clustering developments and in information retrieval, C.J. (Keith) van Rijsbergen (now Glasgow University) was Editor-in-Chief of the Computer Journal from 1993 to 2000. A few of his early papers include the following.


From 2000 to 2007, I was in this role as Editor-in-Chief of the Computer Journal. I wrote in an editorial for the 50th Anniversary in 2007 the following:

“When I pick up older issues of the Computer Journal, I am struck by how interesting many of the articles still are. Some articles are still very highly cited, such as Fletcher and Powell on gradient descent. Others, closer to my own heart, on clustering, data analysis, and information retrieval, by Lance and Williams, Robin Sibson, Jim Rohlf, Karen Spärck Jones, Roger Needham, Keith van Rijsbergen, and others, to my mind established the foundations of theory and practice that remain hugely important to this day. It is a pity that journal impact factors, which mean so much for our day to day research work, are based on publications in just two previous years. It is clear that new work may, or perhaps should, strike out to new shores, and be unencumbered with past work. But there is of course another also important view, that the consolidated literature is both vital and a well spring of current and future progress. Both aspects are crucial, the ‘sleep walking’ innovative element, to
use Arthur Koestler’s [30] characterization, and the consolidation element that is part and parcel of understanding.”

The very first issue of the Computer Journal in 1958 had articles by the following authors – note the industrial research lab affiliations for the most part:

2. E.S. Page
3. D.T. Caminer (Leo Computers Ltd.)
4. R.A. Brooker (Computing Machine Laboratory, University of Manchester)
5. R.G. Dowse and H.W. Gearing (Business Group of the British Computer Society)
6. A. Gilmour (The English Electric Company Ltd.)
7. A.J. Barnard (Norwich Corporation)
8. R.A. Fairthorne (Royal Aircraft Establishment, Farnborough)
9. S.H. Hollingdale and M.M. Barritt (RAE as previous)

Then from later issues I will note some articles that have very clear links with data analysis:

5. In Vol. 4, No. 4, and in Vol. 6, No. 1, there were articles on regression analysis.
5 Conclusions

In this article I have focused on early developments in the data mining or unsupervised view of data analysis. Some of those I have referred to, e.g. Vannevar Bush and Paul Otlet, became obscured or even eclipsed for a while. It is clear however that undisputable progress in the longer term may seem to develop in fits and starts when seen at finer temporal scales. (This is quite commonplace. In literature, see how the centenary of Goethe’s birth in 1848, following his death on 22 March 1832, passed unnoticed. Goethe did not come to the fore until the 1870s.)

What I am dealing with therefore in exploratory, heuristic and multivariate data analysis has led me to a sketch of the evolving spirit of the times. This sketch has taken in the evolution of various strands in academic disciplines, scholarly research areas, and commercial, industrial and economic sectors.

I have observed how the seeds of the present – in fact, remarkably good likenesses – were often available in the period up to 1985 that is mainly at issue in this article. This includes the link between scholarly activity and economic and commercial exploitation. It includes various aspects of the PhD degree.

The consequences of the data mining and related exploratory multivariate data analysis work overviewed in this article have been enormous. Nowhere have their effects been greater than in current search engine technologies. Also wide swathes of database management, language engineering, and multimedia data and digital information handling, are all directly related to the pioneering work described in this article.

In section 4.1 I looked at how early exploratory data analysis had come to play a central role in our computing infrastructure. An interesting view has been offered by [3], finding that all of science too has been usurped by exploratory data analysis, principally through Google’s search facilities. Let us look at this argument with an extended quotation from [3].

‘All models are wrong, but some are useful.’ So proclaimed statistician George Box 30 years ago, and he was right. ... Until now. ....

At the petabyte scale, information is not a matter of simple three- and four-dimensional taxonomy and order but of dimensionally agnostic statistics. It calls for an entirely different approach, one that requires us to lose the tether of data as something that can be visualized in its totality. It forces us to view data mathematically first and establish a context for it later. ...

Speaking at the O’Reilly Emerging Technology Conference this past March [2008], Peter Norvig, Google’s research director, offered an update to George Box’s maxim: ‘All models are wrong, and increasingly you can succeed without them.’ ...

This is a world where massive amounts of data and applied mathematics replace every other tool that might be brought to bear. Out with every theory of human behavior, from linguistics to sociology. Forget taxonomy, ontology, and psychology. Who knows why people do what they do? The point is they do it, and we can track and measure it with unprecedented fidelity. With enough data, the numbers speak for themselves.
The big target here isn’t advertising, though. It’s science. The scientific method is built around testable hypotheses. These models, for the most part, are systems visualized in the minds of scientists. The models are then tested, and experiments confirm or falsify theoretical models of how the world works. This is the way science has worked for hundreds of years.

There is now a better way. Petabytes allow us to say: ‘Correlation is enough.’ We can stop looking for models. We can analyze the data without hypotheses about what it might show. We can throw the numbers into the biggest computing clusters the world has ever seen and let statistical algorithms find patterns where science cannot.”

This interesting view, inspired by our contemporary search engine technology, is provocative. The author maintains that: “Correlation supersedes causation, and science can advance even without coherent models, unified theories, or really any mechanistic explanation at all.”

No, in my view, the sciences and humanities are not to be consigned to any dustbin of history – far from it.

As I wrote in [39], a partnership is needed rather than dominance of one view or another. “Data analysts have far too often just assumed the potential for extracting meaning from the given data, telles quelles. The statistician’s way to address the problem works well sometimes but has its limits: some one or more of a finite number of stochastic models (often handled with the verve and adroitness of a maestro) form the basis of the analysis. The statistician’s toolbox (or surgical equipment, if you wish) can be enormously useful in practice. But the statistician plays second fiddle to the observational scientist or theoretician who really makes his or her mark on the discovery. This is not fair.

Without exploring the encoding that makes up primary data we know very, very little. (As examples, we have the DNA codes of the human or any animal; discreteness at Planck scales and in one vista of the quantum universe; and we still have to find the proper encoding to understand consciousness.) ... [Through correspondence analysis there] is the possibility opened up for the data analyst, through the data encoding question, to be a partner, hand in hand, in the process of primary discovery.”

References


[2] R Adler, J Ewing, P Taylor, *Citation Statistics*, A report from the International Mathematical Union (IMU) in cooperation with the International Council of Industrial and Applied Mathematics (ICIAM) and the Institute of Mathematical Statistics (IMS), Joint Committee on Quantitative Assessment of Research, 11 June 2008
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[38] F. Murtagh, “Multivariate data analysis software and resources”, http://astro.u-strasbg.fr/~fmurtagh/mda-sw


Appendix: Sources for Early Work

- Classification Literature Automated Search Service, a CD distributed currently with the first issue each year of the Journal of Classification. See http://www.classification-society.org/csna

The following books have been scanned and are available in their entirety on the CD.

1. Algorithms for Clustering Data (1988), AK Jain and RC Dubes
2. Automatische Klassifikation (1974), HH Bock
3. Classification et Analyse Ordinale des Données (1981), IC Lerman
4. Clustering Algorithms (1975), JA Hartigan
5. Information Retrieval (1979, 2nd ed.), CJ van Rijsbergen
7. Principles of Numerical Taxonomy (1963), RR Sokal and PHA Sneath
8. Numerical Taxonomy: the Principles and Practice of Numerical Classification (1973), PHA Sneath and RR Sokal

- Les Cahiers de l’Analyse des Données was the journal of Benzécri’s lab from 1975 up to 1997, with four issues per year. Scanning of all issues has started, working chronologically backwards with thus far 1994–1997 covered. See http://thames.cs.rhul.ac.uk/~fionn/CAD

- Some texts by Jean-Paul Benzécri and Françoise Benzécri-Leroy, published between 1954 and 1971, are available at http://www.numdam.org (use e.g. “benzécri” as a search term).