

MA2341 - Advanced Mechanics 1

Michelmas Term - 2015-2016

REVIEW TOPICS

- Mathematical Background:
 - multi-variable calculus, matrix theory
 - cartesian, 2-D polar, 3-D polar, cylindrical coordinates
 - Einstein index/summation notation, Kronecker δ , Levi-Cevita symbols
 - Vector identities
- Essential Topics:
 - Lagrangian, Hamiltonian
 - Hamilton's Principle
 - Euler-Lagrange equations
 - Conserved quantities, cyclic coordinates: Energy, linear momentum, angular momentum.
 - Generalized coordinates and forces
 - Constraints, Lagrange multipliers, Generalized forces of constraint
 - Transformations: rotations, translations, boosts, spatial inversion, time-reversal, Noether's Theorem
 - (pseudo) Scalars, Vectors, and Tensors.
- Calculus of Variations: extremization in the presence of constraints
- One-dimensional motion
 - Allowed regions of motion, turning points
 - Integrating the equations of motion
- Central Force Motion
 - Center of Mass, Reduced Mass
 - Centrifugal barrier, effective potential, turning points
 - Kepler problem, equation for orbits, conic sections
 - conserved quantities, Runge-Lenz vector
- Oscillations
 - Expanding the Lagrangian around stable equilibria, simple harmonic motion

- Coupled oscillations, normal frequencies, normal modes, normal coordinates.
 - Over damped, under damped, critically damped oscillations
 - Retaining more terms in the expansion, anharmonic oscillations
- Rigid Body Motion
 - Moment of Inertia tensor
 - Parallel axis theorem
 - Principal moments, Principal axis
 - Rotational motion, body coordinates
 - Precession, nutation
- Motion in non-inertial frames
 - Centrifugal force
 - Coriolis force